

# Calculations on a Network Model

## Supplemental Material for Construction Management: Planning and Scheduling

The following information outlines the basic steps required to run calculations on a Precedence Network to determine *Early Start* and *Early Finish*, *Late Start* and *Late Finish*, *Float*, and to identify the *Critical Path*. This discussion uses a beginning-of-day convention whereby each activity starts and ends on the beginning of the listed day; i.e. if an item begins on Day 10 and has a duration of 1 Day, it will begin on Day 10 and end on Day 11. All relationships used in this discussion are Start-to-Finish relationships.

1. **Assign *Early Start (ES)* and *Early Finish (EF)***
  - a. Begin by assigning Day 1 as the *Early Start* day of the first activity
  - b. Calculate the *Early Finish* for this activity by adding its *Duration* to its *Early Start* ( $EF = ES + \text{Duration}$ )
  - c. The next activity on the network is assigned an *Early Start* that is equal to the *Early Finish* of its Immediately Preceding Activity (IPA)
    - i. In Figure 1 – The first activity begins on Day 1 and has a Duration of 2 days, so its *Early Finish* is the beginning of Day 3, meaning the next activity can start at the beginning of Day 3 – remember when doing this by hand to stick with a single convention (in this case beginning-of-day) when referring to activities

### Terms & Definitions

**Early Start (ES)** – the earliest time that an activity can start based on the latest of the Early Finish times of all its IPA's

**Early Finish (EF)** – the earliest time that an activity can finish, calculated by adding the activity's Duration to its Early Start ( $EF = ES + \text{Duration}$ )

**Late Start (LS)** – the latest time that an activity can start without delaying the completion of the project, calculated by adding the Float of an activity to its Early Start ( $LS = ES + \text{Float}$ )

**Late Finish (LF)** – the latest time that an activity can be finished without delaying the completion of the entire project, calculated by adding the activity's Float to its Early Finish ( $LF = EF + \text{Float}$ )

**Duration** – the value assigned to an activity that represents the time it will take to complete that activity

**Float** – the amount of time that an activity can be delayed before it impacts the completion date of the project (also referred to as Total Float)

**Lag** – the amount of time that exists between the Early Finish of an activity and the Early Start of its successor activity ( $LAG_{AB} = ES_B - ES_A$ )

**Critical Path** – the sequence of linked activities for which the Float value of each activity in the path is zero

- d. If an activity has more than one IPA, its *Early Start* is the latest of the *Early Finish* days of all of its IPA's
- e. Repeat this process making a complete forward pass through the entire network
  - i. At the end of this step, all activities should have *Early Start* and *Early Finish* calculated

**2. Calculate *Lags* for each link**

- a. Each activity should be linked to one or more predecessors (IPA's) unless it is the first activity on the project
- b. Each activity should be linked to a successor activity unless it is the last activity to be completed on the project
  - i. A construction project will typically need a final activity in the schedule to represent demobilization; things like clean-up and hauling off equipment and trash. Ideally, all other activities should be finished before this final activity is started.
- c. Calculate the *Lag* for each link by determining the difference between the *Early Start* of each activity that follows a link line, and the *Early Finish* of the activity that precedes it - *Lags* must be either 0 or a positive number
  - 1. In Figure 1 – the *Early Start* of the Activity that follows “Inst Net Hardware” is Day 23 (Clean/Move Out) and the *Early Finish* of “Inst Net Hardware” is Day 13, so the *Lag* is 10 ( $Lag_{AB} = ES_B - EF_A$ )
- d. Repeat this process for each link in the network

**3. Calculate *Float* for each activity in the network (also referred to as *Total Float*)**

- a. Begin by assigning a *Float* value of 0 to the last activity in the network
- b. Calculate the *Float* value of that activity's IPA(s), by adding its *Float* value to the value of the connecting Lag line(s)
  - i. In Figure 1 – The last activity is “Clean/Move Out”, and it has three IPA's: “Landscape”, “Inst Net Hardware”, and “Inst Benches”.
    - 1. The *Float* value of “Landscape” is calculated by adding the *Float* value of “Clean/Move Out” (0) to the *Lag* value of the link line connecting the two activities (0) – in this case *Float* for “Landscape” is  $0 + 0 = 0$
    - 2. The *Float* value of “Inst Net Hardware” =  $0 + 10 = 10$
    - 3. The *Float* value of “Inst Benches” =  $0 + 8 = 8$
- c. Repeat this process making a complete backwards pass through the network
  - i. At the end of this step, all activities should have a value (either 0 or a positive number) entered for *Float*

**4. Calculate *Late Start* and *Late Finish***

- a. Begin with the first activity in the network model – calculate its *Late Start* by adding the *Float* value to its *Early Start* ( $LS = ES + Float$ ) – Calculate its *Late Finish* by adding the *Float* value to its *Early Finish* ( $LF = EF + Float$ )
- b. Repeat this process for each activity, making a complete forward pass through the network

**5. Identify the *Critical Path***

- a. Determine the *Critical Path* by identifying the sequence of linked activities for which the *Float* value for each activity in the sequence is 0

- i. In Figure 1 – The *Critical Path* consists of five activities: “Place Concrete”, “Surfacing/Coating”, “Install Fence”, “Landscape”, “Clean/Move Out”
1. “Inst Net Hardware” and “Inst Benches” are not in the *Critical Path* – they have *Float* and can move by the number of days equal to the *Float* without effecting the completion time of the project

**6. Assign Dates to each activity**

- a. The values currently entered in the network model are days; i.e. Day 1, Day 2, Day 3, etc. – To turn the network model into a schedule, these vales need to be converted to dates on a calendar
- b. This conversion from Working Days to dates on a calendar will depend on the definition of a Working Day for the project, and on the planned start date for the project – In other words, if Day 1 is Monday, Day 2 is Tuesday, etc., Day 6 might be Saturday or it might be the following Monday depending on the plan of for the project – Similarly, Day 1 could be any day of the week that is chosen for the start date of the project, it’s not necessarily always a Monday

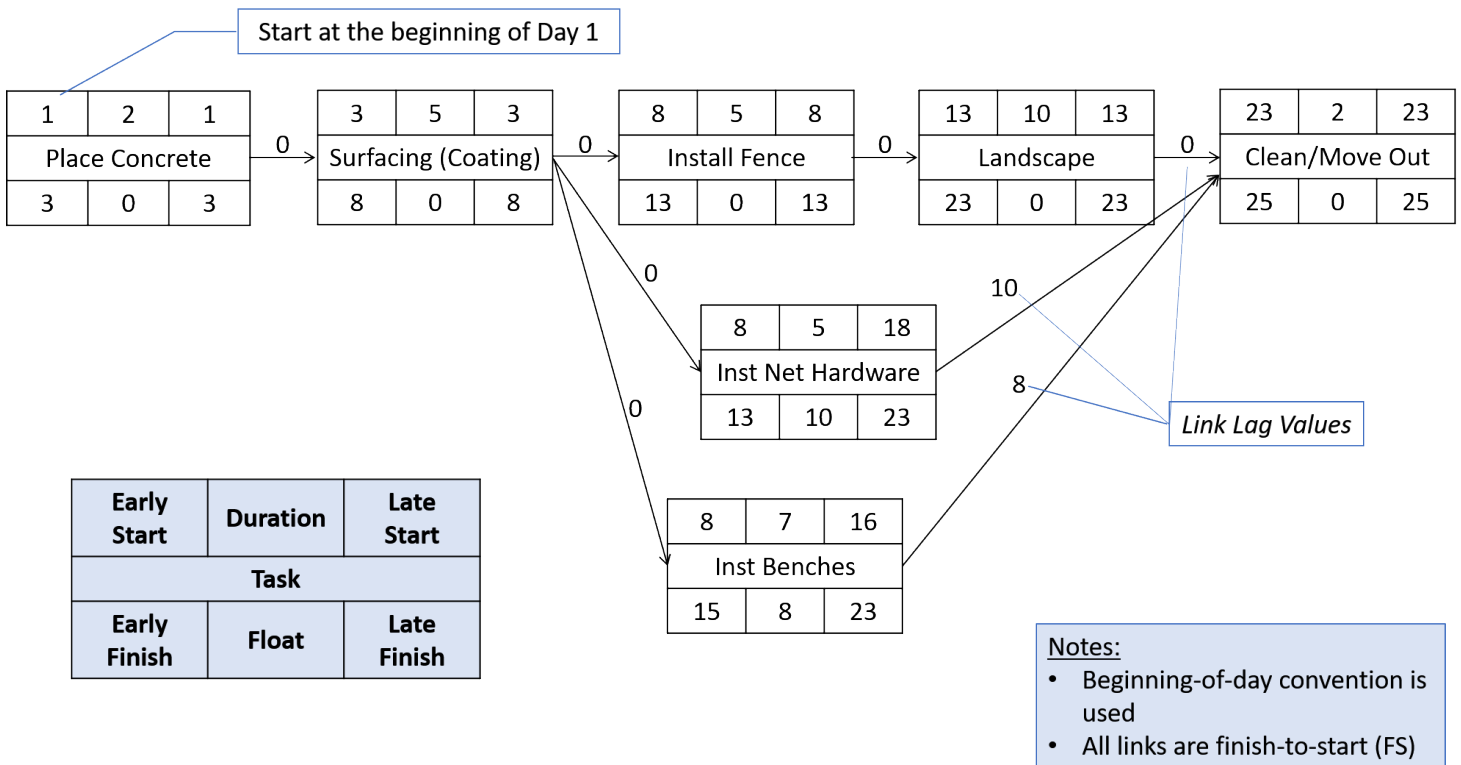


Figure 1 – Calculations on a Precedence Network